

# HMH Into Math<sup>®</sup>

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# GRADE 3

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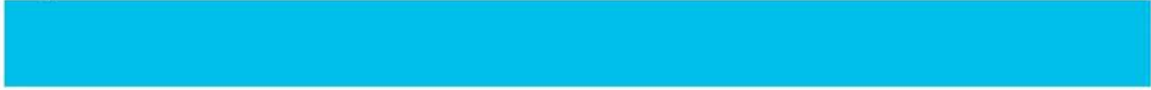
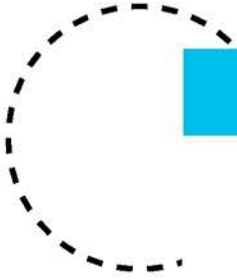
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Module 14

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Module 16

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# GRADE 5

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- use place value to represent whole numbers and decimals.
- use powers of 10 and exponents.
- compare and order decimals to thousandths.

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# GRADE 5

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- apply properties of addition for sums and differences of fractions.
- model sums and differences of fractions with equations.

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- divide unit fractions by whole numbers.
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- assess the reasonableness of decimal sums and differences.
- use place-value strategies and properties of operations to add and subtract decimals.



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- write and plot ordered pairs.
- identify and describe patterns in data.



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- estimate and find the volume of a right rectangular prism.
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- convert measurement units to solve multistep problems.
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